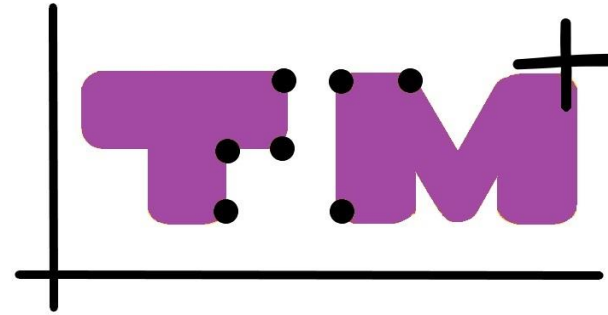
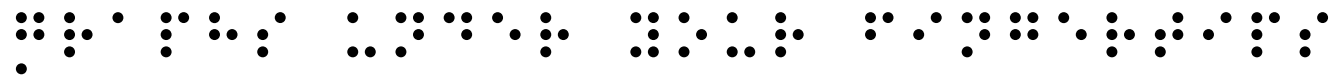




Funded by the  
European Union



# Graphs under your fingertips

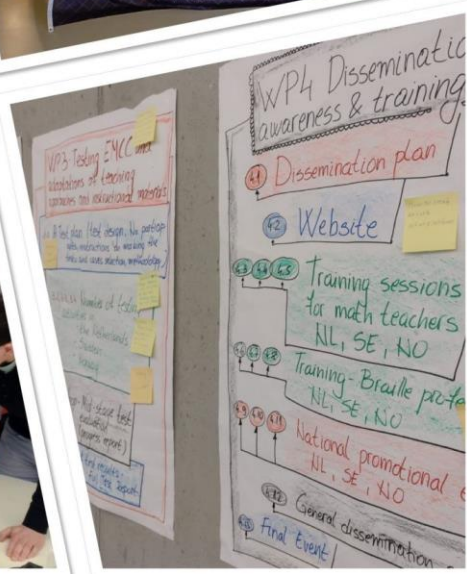
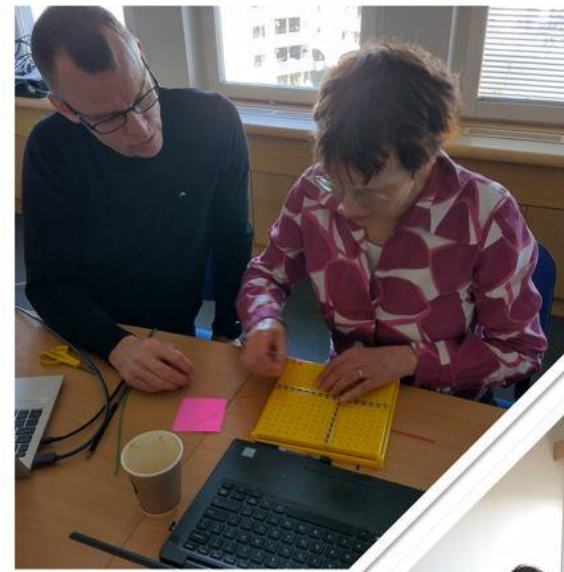


Getting In Touch With Literacy  
November 29 – December 2, 2023  
St. Pete Beach, Florida

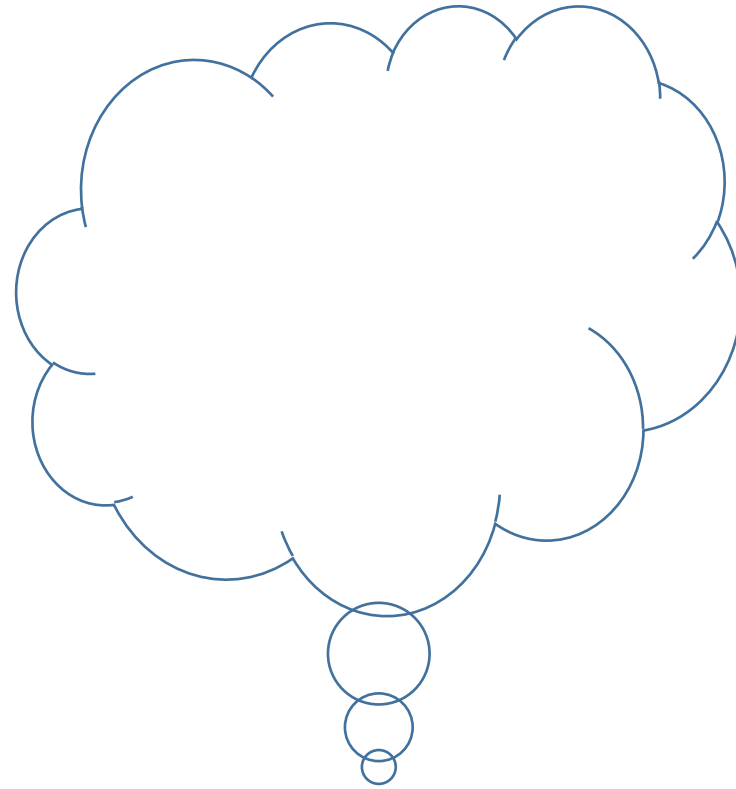




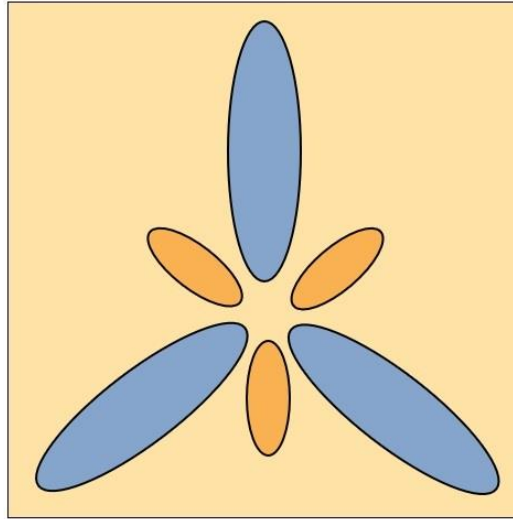
# Participants TouchingMaths+



# Experience verbal description

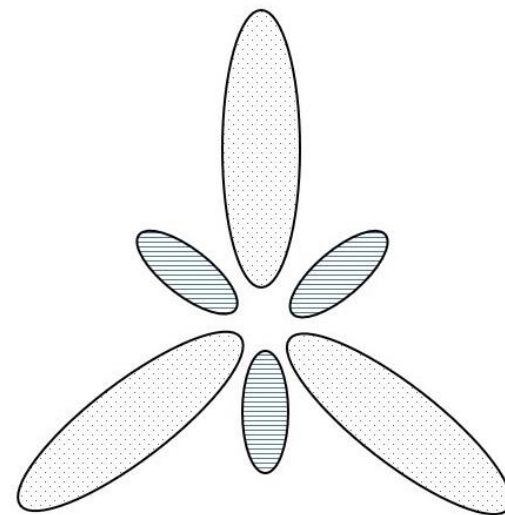
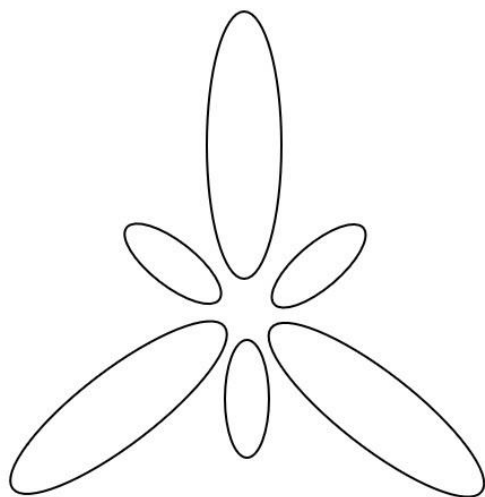


Instructor



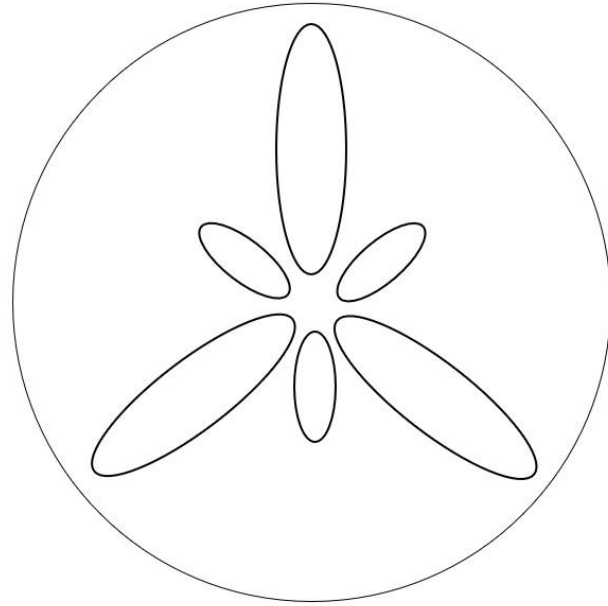
3 types of descriptions:

a) Very detailed descriptions that often include unnecessary information



3 types of descriptions:

b) A description that omits redundant information



3 types of descriptions:

c) A description that omits redundant information and uses mathematical language. Sometimes some extra information is even added.

3 identical small and 3 identical large elliptical figures are placed in a circle in such a way that the figure is rotationally symmetrical with a rotation angle of 120 degrees. The rotation point is the center of the circle.

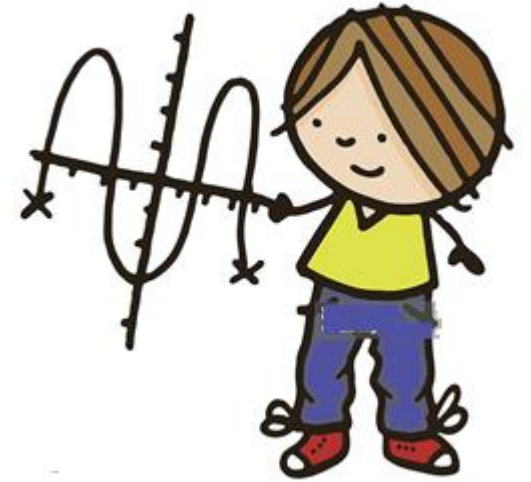
What characteristics should a description of a tactile drawing or 3D model possess?

This depends on:

- The purpose of the assignment.
- The skills and knowledge of the teacher and student involved.
- The intended purpose of the description.
  - There are essential questions that need to be addressed in this context:
    - Is the description meant to replace the tactile drawing or 3D model?
    - Is it intended to complement, reinforce, or reiterate the information presented in the tactile drawing or 3D model?



## Relation with our project



As you can see, it is not that easy to *properly describe* a drawing.

That is one of the reasons why we started our project.

We want to support mathematics teachers and other professionals, among other things, to become more skilled in correctly describing graphs, drawings and 3D models *in mathematical language*.

# EMCC

## The Extended Mathematical Core Curriculum

Our project is about developing an Extended Mathematical Core Curriculum.

# EMCC

## The Extended Mathematical Core Curriculum

The questions we aim to address are as follows:

- *What* additional knowledge and skills do Braille readers need to acquire, beyond those required by sighted students, in order to meet the learning objectives outlined in the Mathematical Core Curriculum (MCC)?
- *How* can they obtain this additional knowledge and these skills?

# EMCC

## The Extended Mathematical Core Curriculum

Final products:

Description of EMCC for graphs, equations and computational thinking / programming.  
This involves:

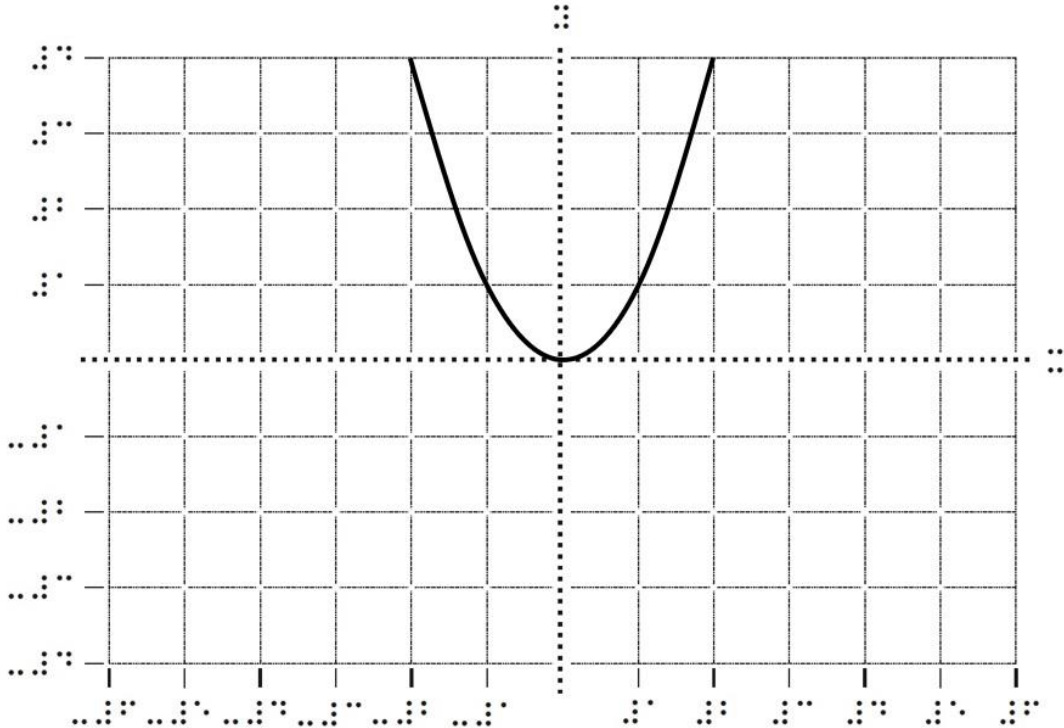
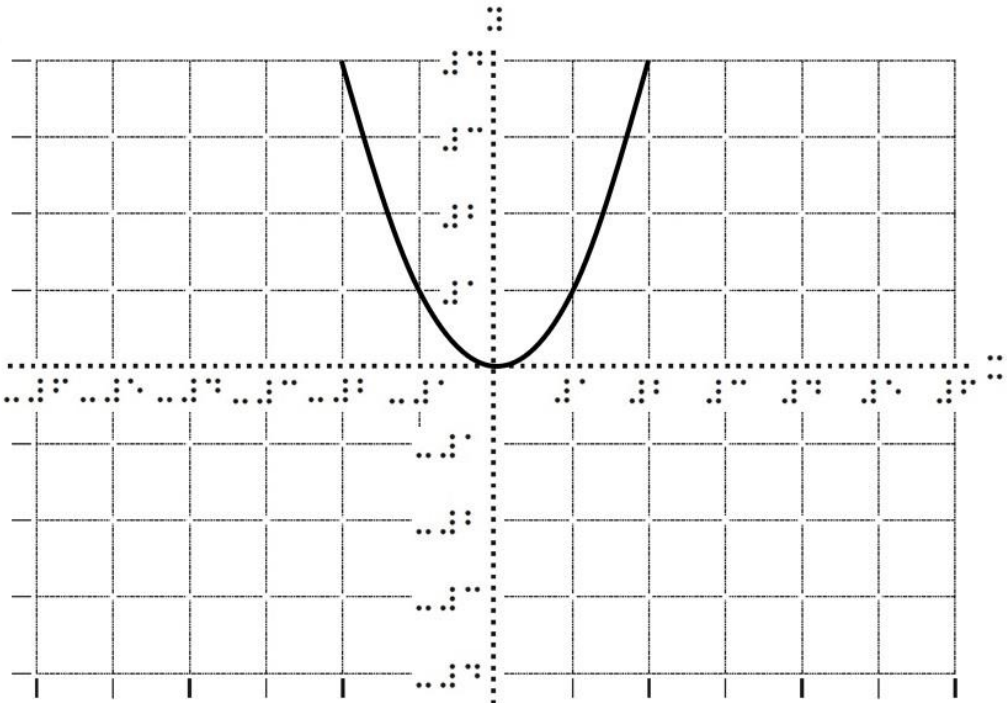
- Instruction guide on braille reading, tactile reading and ICT-skills
- Instruction guide for math teachers
- Learning Resources Document for Braille Readers

# EMCC

## The Extended Mathematical Core Curriculum

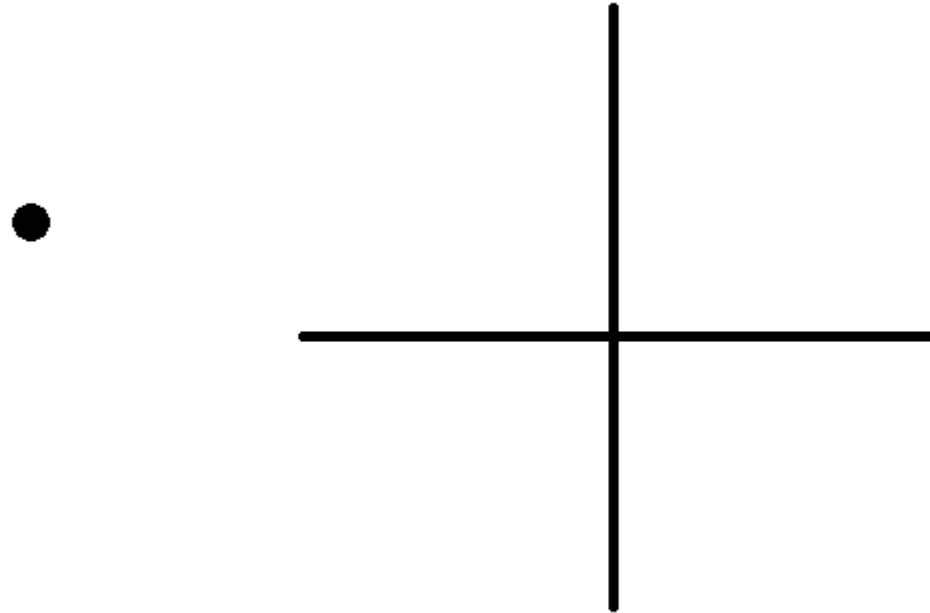
Today the focus is on the EMCC for graphs.

# Instruction on braille reading and tactile reading



# Special materials

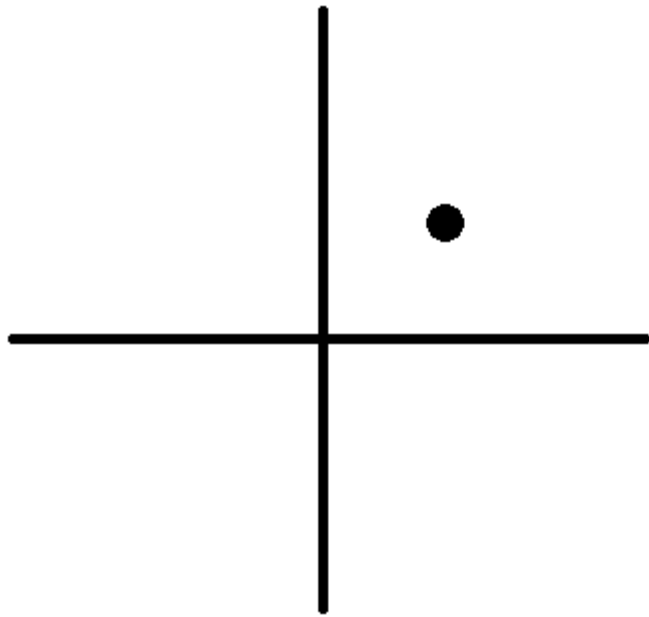
## Special materials movable axes



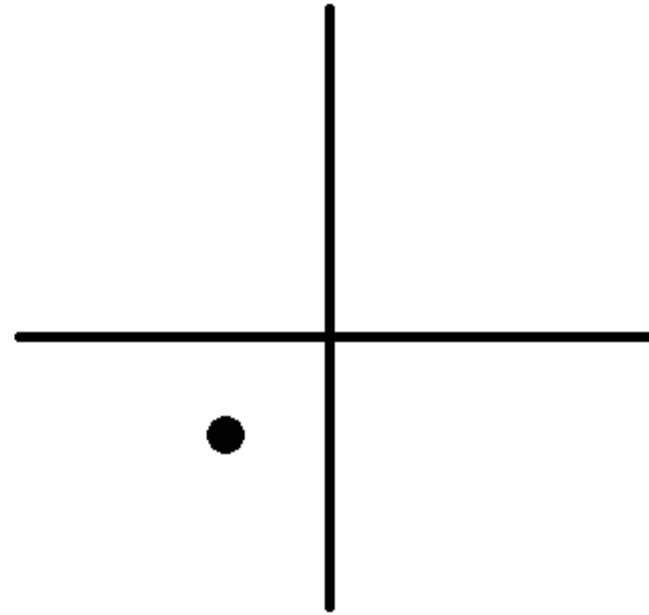
The figure shows a (tangible) point A and a coordinate system with movable axes.

# Special materials

movable axes



$$A = (1; 1)$$

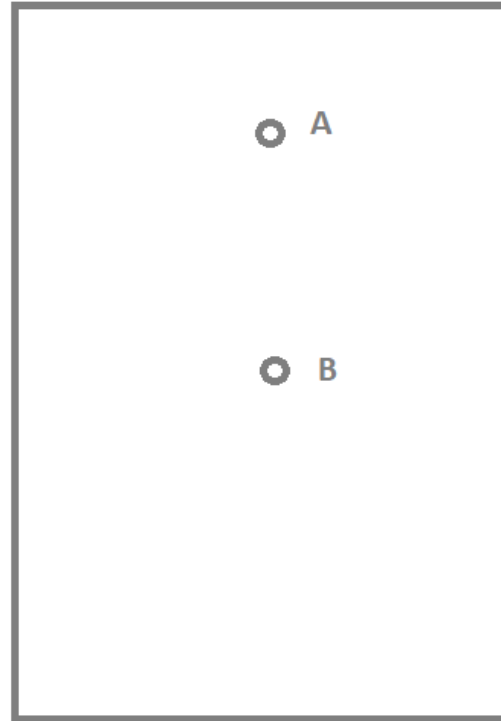


$$A = (-1; -1)$$



## Exercise

- Draw points A and B on a piece of paper so that point A is directly below point B.

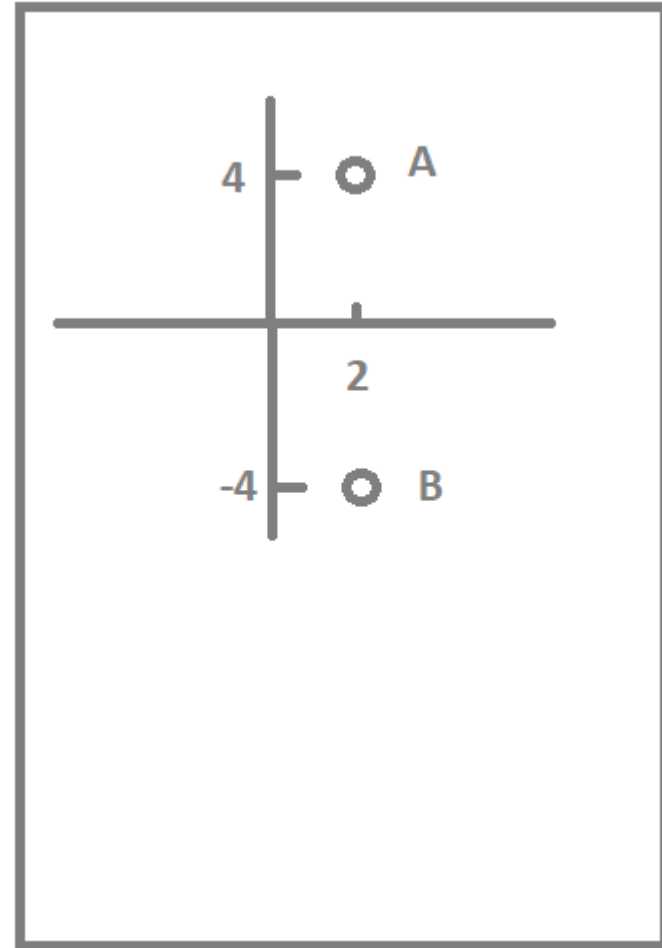
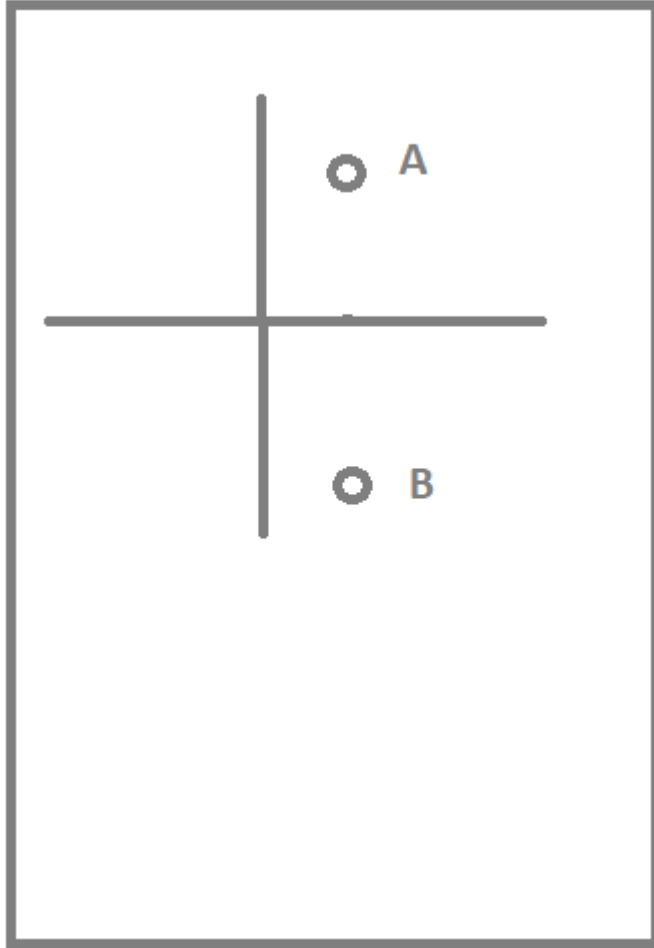


## Exercise

Draw a coordinate system on a sheet of paper such that  
 $A = (2, 4)$  and  $B = (2, -4)$ .



## Exercise



$$A = (2; 4) \text{ and } B = (2; -4)$$

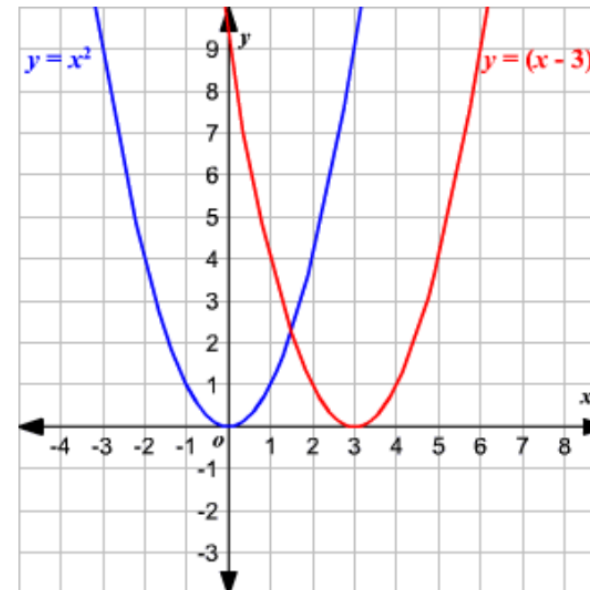
# Instruction guide for math teachers

The math teacher:

- 1) needs to understand how the use of the devices of the Braille reader influences the teaching and learning and must anticipate that.
- 2) is primarily responsible for the math education of the Braille reader.

Much attention for transformations

Much attention for inclusion



# Instruction guide for math teachers

## Adapted instructional materials

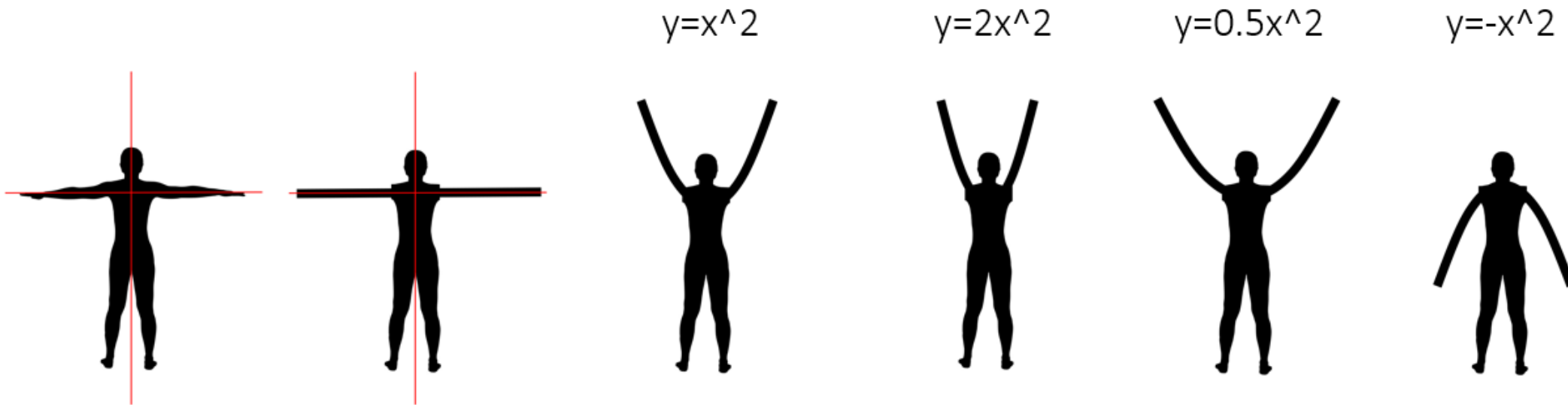
We developed instructional materials tailored for mathematics teachers who instruct Braille readers.

Crucial point of attention

Inclusive education

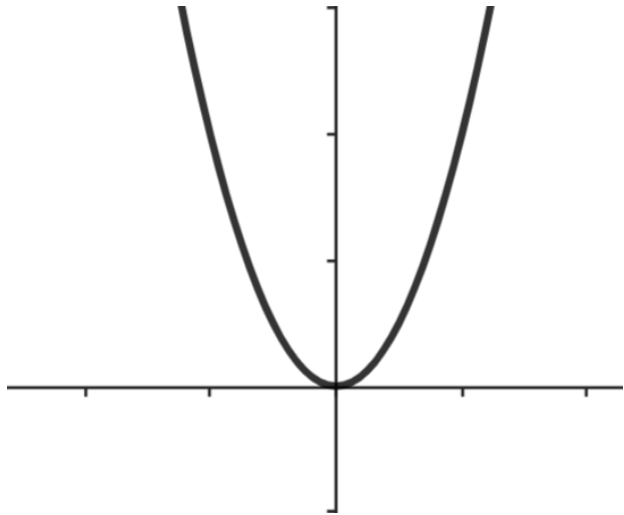
Example: coordinate systems with moving axes.

# Body-graphs



x-axis is on chest height, y -axis is a vertical line from your head to your feet.

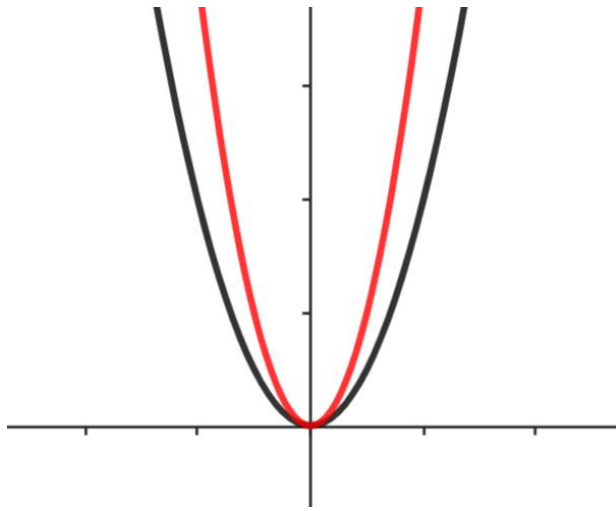
$$y = x^2$$



Standard

$$y = x^2$$

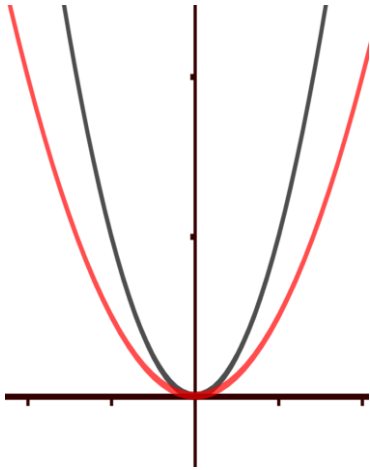




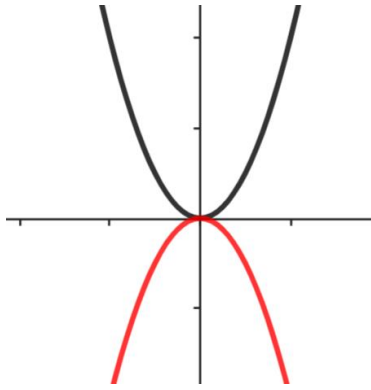
Smaller

$$y = 2x^2$$

Wider

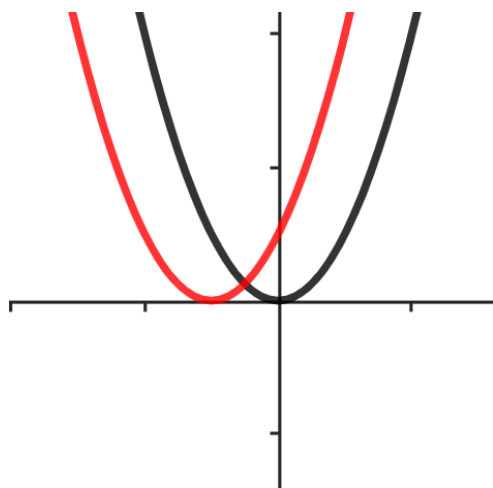


$$y = 0.5 x^2$$



Valley, standard

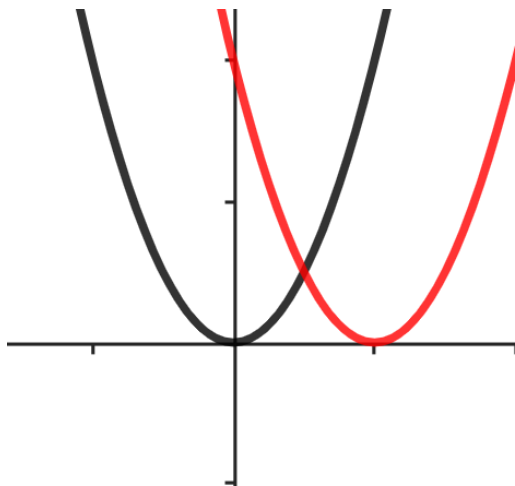
$$y = -x^2$$



Standard

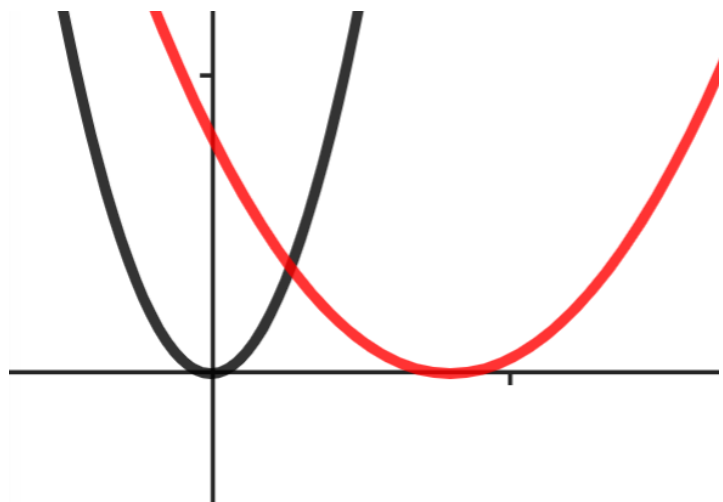


$$y = (x + 1)^2$$



Standard  
Right 

$$y = (x - 2)^2$$



Wider  
Right



$$y = (0.5x - 2)^2$$

Finally

$$y = 0.2 x^2 \rightarrow y = 0.4 x^2 \rightarrow y = 0.6 x^2 \rightarrow y = 0.8 x^2 \rightarrow y = 1 x^2 \\ \rightarrow y = 2 x^2 \rightarrow y = 4 x^2 \rightarrow y = 6 x^2 \rightarrow y = 8 x^2 \rightarrow 10 x^2$$

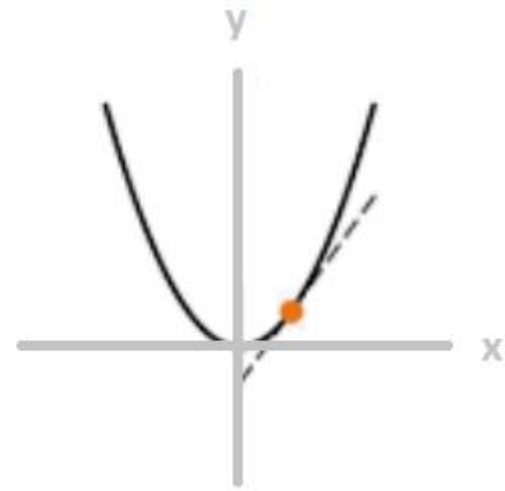
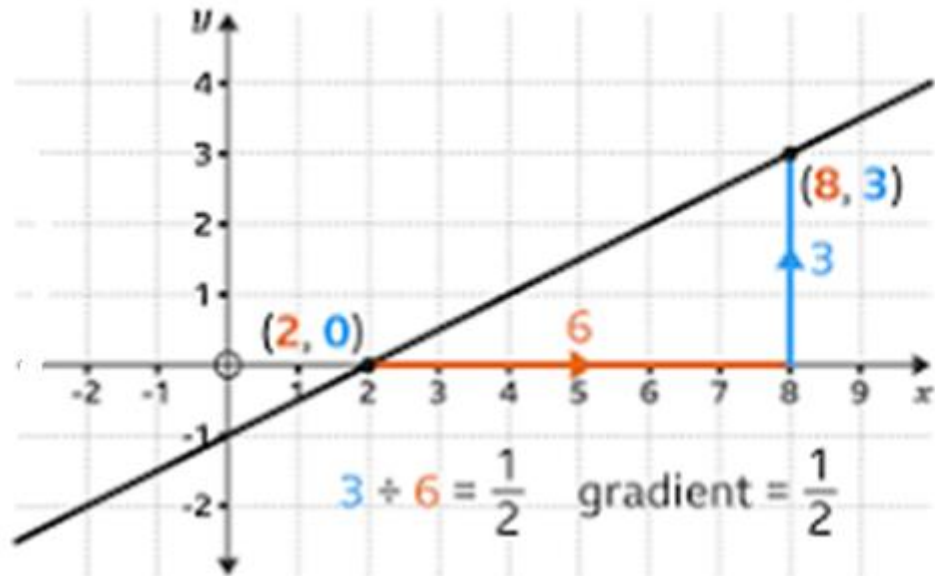
Applause for yourself



Start Body Graph Dancing



# Gradient



Melody: row row row the boat



Annemiek: I don't hear anything?????

The gradient

Gradient of a line is easy to define

Gradient is the measure of the steepness of a line

Gradient of a line is simple to be found

Change in y over change in x and that's the gradient

Website Tjorborn (think about a good transition)